

## CMSACOR04T-COMPUTER SCIENCE (CC4)

## **DISCRETE STRUCTURES**

Time Allotted: 2 Hours

Full Marks: 50

 $2 \times 5 = 10$ 

The figures in the margin indicate full marks. Candidates should answer in their own words and adhere to the word limit as practicable. All symbols are of usual significance.

## Answer Question No. 1 and any *five* from the rest

- 1. Answer any *five* questions from the following:
  - (a) What do you mean by uncountably infinite set? Give an example.
  - (b) A set S has n elements. Prove by mathematical induction that it has  $2^n$  sub-sets.
  - (c) What do you mean by a reflexive relation? Give an example.
  - (d) If *P* and *Q* are two propositions, prove that  $(((P \lor Q) \multimap P) \text{ is a tautology.}$
  - (e) Find out the number of distinguishable arrangements of the word GOOGLE so that two O's are always together.
  - (f) Show that number of odd degree vertices in a graph is always even.
  - (g) Define a complete graph.
  - (h) Prove that the maximum number of edges possible in a simple graph with *n* vertices is  $\frac{n(n-1)}{2}$ .
  - (i) What is chromatic number of a graph?
  - (j) Derive the Big-Oh notation of the function  $f(x) = x^2 + x \log x + 100$ .

2.	(a)	A string like 12321, which reads the same forward and backward, is called a palindrome. How many palindromes can be made using characters from {0, 1, 2, 3,, 9} using (i) five digits, (ii) six digits?	4
	(b)	Suppose a programming language allows its variable-names to be maximum six- character long. Characters can be from the set { $A - Z$ , $a - z$ , $0 - 9$ , _}. The first character must be an alphabet or '_'. How many distinct names are there?	4
3.	(a)	What is meant by time complexity of an algorithm? Formulate the recurrence relation to find out the time complexity of Binary search.	4

(b) Solve the recurrence relation formulated by you using the method of substitution.

4

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- 4. (a) Define generating function of a sequence  $\{a_n\}$ . Find out the Generating Function for the infinite sequence  $\{a_n = (n+1), \text{ for } n \ge 0\}$ .
  - (b) Solve the *linear recurrence relation*, subject to the initial conditions  $x_0 = 0$ ,  $x_1 = 1$ :

3

5

3

5

3 5

4

3

5

$$x_{n+2} + 2x_{n-1} - 15x_n = 0$$
,  $n \ge 2$ 

- 5. (a) State the Principle of Inclusion and Exclusion (PIE) for four sets A, B, C, D.
  - (b) Find out the number of primes between 1 and 100 using PIE.
- 6. (a) Distinguish between a graph and a multi-graph.
  - (b) Compare between the adjacency matrix and the adjacency list representation of a graph. Illustrate with the following graph with vertex-set and edge-set {a, b, c, d} and {1, 2, 3, 4} respectively.



- 7. (a) What is a minimally connected graph? Prove that a minimally connected graph is 4 a tree.
  - (b) What is a spanning tree? Find out two distinct spanning trees of the following graph.



- 8. (a) Compare between an Eulerian graph and a Hamiltonian graph.
  - (b) Draw graphs which are
    - (i) Both Eulerian and Hamiltonian
    - (ii) Eulerian but not Hamiltonian
    - (iii) Hamiltonian but not Eulerian.
    - **N.B.**: Students have to complete submission of their Answer Scripts through E-mail / Whatsapp to their own respective colleges on the same day / date of examination within 1 hour after end of exam. University / College authorities will not be held responsible for wrong submission (at in proper address). Students are strongly advised not to submit multiple copies of the same answer script.

